Amendments to the claims

This listing of claims will replace all prior versions, and listings, of claims in the application:

Listing of Claims:

- 1. (original) A method of fragile watermarking, characterised by the step of generating at least a first ill-conditioned operator, said ill-conditioned operator being related to values extracted from an image or portion thereof A.
- 2. (original) A method of fragile watermarking according to claim 1 wherein the ill-conditioned operator is generated by altering a value to increase the operator's condition number.
- 3. (currently amended) A method of fragile watermarking according to claim 1-or-2, comprising the step of replacing a non-zero singular value of a singular value matrix S_A of an image or portion thereof A, with a solution to a linear equation comprising the ill-conditioned operator, wherein the non-zero singular value to be replaced is the smallest non-zero singular value S_A of rank r.
- 4. (canceled)
- 5. (currently amended) A method of fragile watermarking according to claim 1 any one of the preceding claims, wherein a non-zero singular value of a singular value matrix S_W of a watermark pattern or portion thereof W is replaced, such that said replacement increases the condition number of the singular value matrix S_W of the watermark pattern or portion thereof W, wherein the non-zero singular value to be replaced is the smallest non-zero singular value $S_t(W)$ in a singular value matrix S_W of rank t.
- 6. (canceled)

7. (currently amended) A method of fragile watermarking according to claim 5 any one of the preceding claims, wherein the step of calculating a replacement non-zero singular value of singular value matrix S_W of a watermark or portion thereof W is calculated by comprises calculating substantially the following equation part:

$$s_{t}(W) = \varepsilon$$
,

where ε is a small positive real number that increases the condition number of the singular value matrix S_w .

8. (currently amended) A method of fragile watermarking according to <u>claim 1</u>-any one of the preceding claims, wherein the step of generating at least a first ill-conditioned operator comprises calculating substantially the following equation part:

$$B = \hat{A}\hat{W},$$

where \hat{W} is substantially constructed according to $\hat{W} = U_w \hat{S}_w V_w^T$, \hat{S}_w comprising at least one altered singular value $S_t(W) = \varepsilon$, and such that B forms a parametric family of matrices $B(\hat{S}_r) = \hat{A}(\hat{S}_r)\hat{W}$ for possible values of $\hat{S}_r(A)$.

- 9. (currently amended) A method of fragile watermarking according to claim 8, wherein $\frac{s_r(A)}{s_r(A)} \cdot \frac{\hat{s}_r(A)}{s_r(A)}$ is determined by an L₂-norm solution of the least squares problem $\frac{\min}{x \in \Re^p} \|Bx b\|_2^2$ to equal the square of a predefined key N of predetermined value, where b is an arbitrary vector.
- 10. (currently amended) A method of fragile watermarking according to <u>claim 3</u> any one of the preceding claims, wherein the step of calculating the replacement non-zero singular value of singular value matrix A is calculated by comprises calculating substantially the following equation part:

$$\min_{\hat{\boldsymbol{S}}_{r}(\boldsymbol{A})} \left\{ \sum_{i=1}^{q} \left(u_{B_{i}}^{T} b / s_{i} (B(\hat{\boldsymbol{S}}_{r})) \right)^{2} - N^{2} \right\},$$

where u_{B_i} is the I-th column of the matrix formed with the right singular vectors of B.

11. (original) A method of fragile watermarking according to claim 10, wherein $\hat{s}_r(A)$ further satisfies

 $\hat{s}_r(A) = \overline{s}_r(A) \in [\max(eps, s_r(A) - \delta), s_r(A) + \delta] = [H_0, H_1],$ where δ is a distortion control and eps is machine precision, such that the step of calculating the replacement non-zero singular value comprises calculating substantially the following equation part:

with all terms as defined herein.

- 12. (canceled)
- 13. (original) A method of fragile watermarking according to claim 12, wherein for a sequential watermarking process comprising the watermarking of portion $A^{(k)}$ after the watermarking of portion $A^{(k-1)}$, k=1,...,L of L portions, then the step of calculating $b^{(k)}$ for portion $A^{(k)}$ comprises calculating substantially the following equation part:

$$b^{(k)} = egin{cases} A^{(k)}Z^{(k)} & & for \ k = 1 \ A^{(k-1)}Z^{(k)} & & else \end{cases},$$

where Z(k) is a pseudo-random binary vector.

14. (currently amended) A method of fragile watermarking according to claim 1 any one of the preceding claims, wherein the step of calculating a the watermarked image or portion thereof \hat{A} comprises calculating substantially the following equation part:

$$\hat{A} = U_A \hat{S}_A V_A^T$$

where \hat{S}_A comprises at least one replaced singular value, U_A and V_A being left and right singular matrices.

15. (currently amended) A method of fragile watermarking according to <u>claim 1</u> any one of the preceding claims, wherein a watermark pattern or portion thereof *W* is generated by a pseudo-random generator seeded by a key *K* of predetermined value.

- 16. (canceled)
- 17. (currently amended) A method of fragile watermarking according to <u>claim 15</u>-either one of claims 15 and 16, wherein the a watermark pattern or portion thereof W is generated by a pseudo-random generator seeded by a key K of predetermined value, combined with either a single or repeated instance of a logo.
- 18. (currently amended) A method of fragile watermarking according to <u>claim 1</u> any one of the preceding claims, comprising the following steps;
 - i. generating a K-dependent watermark pattern W from Ω , or recalling a pre-existing one;
 - ii. constructing a parametric family of matrices $B(\hat{s}_r)$;
 - iii. estimating a unique parameter $\overline{S}_r(A)$, that minimizes the expression

$$\frac{\min}{\hat{s}_r} \left\{ \sum_{i=1}^q \left(u_{B_i}^T b / s_i (B(\hat{s}_r)) \right)^2 - N^2 \right\}; \text{ and}$$

iv. estimating the watermarked block $\hat{A} = U_A \hat{S}_A V_A^T$ by setting

$$\hat{S} = diag(s_1(A), \ldots, s_{r-1}(A), \overline{s}_r(A)).$$

- 19. (currently amended) A method of fragile watermarking according to <u>claim 1</u>-any-one of elaims 1 to 17, comprising the following steps;
 - i. generating a K-dependent watermark pattern W from Ω , or recalling a pre-existing one;
 - ii. constructing a parametric family of matrices $B(\hat{s}_r)$;
 - iii. estimating a unique parameter $\overline{s}_r(A) \in \left[\max{(eps,\,s_r(A)\,-\,\delta)}\;,\,s_r(A)\,+\,\delta\right] = \left[H_0\,,\,\,H_1\right], \text{ that minimizes the expression:}$

$$\min_{\hat{S}_{r} \in [H_{0}, H_{1}]} \left\{ \sum_{i=1}^{q} \left(u_{B_{i}}^{T} b / s_{i} (B(\hat{s}_{r})) \right)^{2} - N^{2} \right\}; \text{ and}$$

- iv. estimating the watermarked block $\hat{A} = U_A \hat{S}_A V_A^T$ by setting $\hat{S} = diag(S_1(A), \dots, S_{r-1}(A), \overline{S}_r(A))$.
- 20. (original) A method of verifying a fragile watermark, characterised by the step of generating at least a first ill-conditioned operator by altering a value to increase its condition number, said ill-conditioned operator being related to values extracted from a received image or portion thereof A^* .
- 21. (original) A method of verifying a fragile watermark according to claim 20, characterised by the step of calculating a solution to the least squares problem

$$\min_{\mathbf{X} \in \mathfrak{R}^p} \| \mathbf{B}^* \mathbf{X} - \mathbf{b} \|_2^2 \text{ where } \mathbf{B}^* = \mathbf{A}^* \hat{\mathbf{W}}.$$

22. (currently amended) A method of verifying a fragile watermark according to claim 20 either one of claims 20 and 21, wherein a positive square-root N^* of the L₂-norm solution of the least squares problem $\lim_{x \to \infty} \|B^*x - b\|_2^2$ is compared with key N; and

the received image or portion thereof A^* comprising the fragile watermark is declared authentic if $\left|N^*-N\right| \leq \tau$, where τ is a threshold value.

23. (currently amended) A method of verifying a fragile watermark according to claim 22 any one of claims 20 to 22, wherein the step of calculating value N^* is calculated by comprises calculating substantially the following equation part:

$$(N^*)^2 = \sum_{i=1}^n \left(u_{B_i}^T b / s_i(B^*) \right)^2;$$

 N^* is compared with key N; and

the received image or portion thereof A^* comprising the fragile watermark is declared authentic if $|N^* - N| \le \tau$, where τ is a threshold value.

24. (currently amended) Apparatus for fragile watermarking of an image in accordance with a method of <u>claim 1</u>-any one of claims 1 to 19, and comprising;

generating means for generating at least a first ill-conditioned operator, said ill-conditioned operator being related to values extracted from an image or portion thereof A.

25. (currently amended) Apparatus for validating a fragile watermarked image in accordance with a method of claim 20 any one of claims 20 to 23, and comprising;

generating means for generating at least a first ill-conditioned operator by altering a value to increase its condition number, said ill-conditioned operator being related to values extracted from a received image or portion thereof A^* .